

FIG. 1

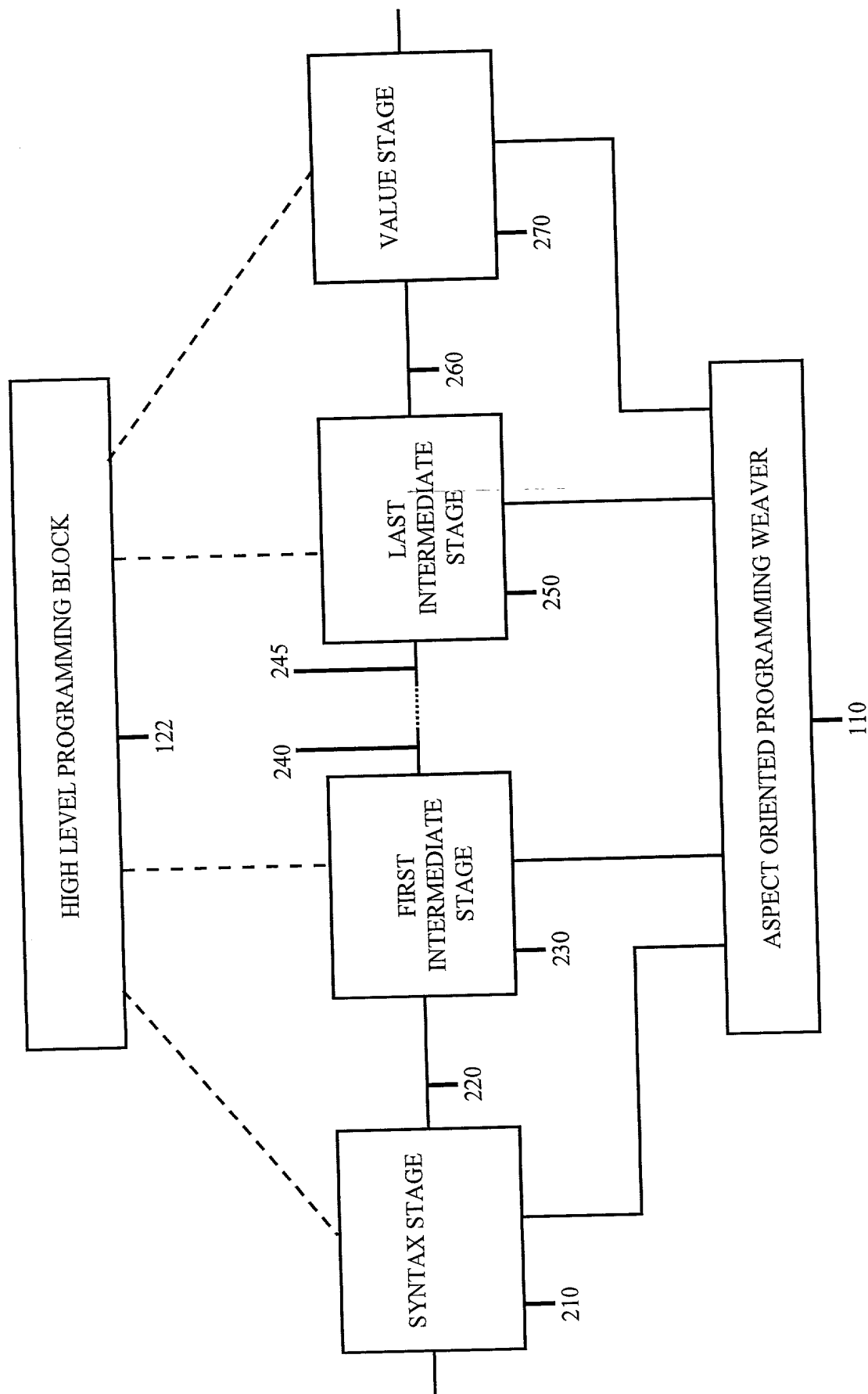


FIG. 2

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1  (stage requested-loops)
2  (projection key :defined-on requested-loops)
3  (projection computing-loop :defined-on requested-loops)
4  (define test
5    (lambda (x y z)
6      (and! (and! X y) z)))
7  (define and!
8    (reduction-stage requested-loops
9      (lambda (arg1 arg2)
10        (pointwise #'and arg1 arg2))))
11 (propagator requested-loops :bottom-up
12   (lambda (term)
13     (case requested-loops term
14       ((pointwise op arg1 arg2) (op arg1 arg2)
15        (let ((starting-loop
16              (fuse-loops (get-or-make-loop arg1) (get-or-make-loop arg2))
17                        (my-key (gensym)))
18              (deconstruct requested-loops starting-loop
19                (ptw-loop fn inputs outputs) (fn inputs outputs)
20                (let* ((new-fn (reduction-stage computation
21                              (lambda (args)
22                                (let* ((temp (fn args))
23                                      (result
24                                        (op (find (key arg1) temp)
25                                              (find (key arg2) temp))))
26                                  (cons (cons my-key result)
27                                        temp))))
28                  (new-loop (defer (ptw-loop new-fn inputs outputs))))
29                (update (key value) my-key)
30                (update (computing-loop value) new-loop))
31                (if (computing-loop arg1)
32                    (update (computing-loop arg1)
33                            (defer (loop-reference value))))
34                (if (computing-loop arg2)
35                    (update (computing-loop arg2)
36                            (defer (loop-reference value))))))))
37     (else (note-demands value)
38           )))
39

```

FIG. 3A

```

39  (define get-or-make-loop (value)
40    (if (and (same-frequency value) (computing-loop value))
41        (get-loop value)
42        (defer (ptw-loop
43                (reduction-stage computation
44                  (lambda (args) args)
45                  (list (cons (key value) value))
46                      nil))))))
47  (define get-loop
48    (reduction-stage computation
49      (lambda (value)
50        (computing-loop (get-loop-location value))))))
51  (define get-loop-location
52    (reduction-stage computation
53      (lambda (value)
54        (case requested-loops (computing-loop value)
55          ((loop-reference next) (next)
56           (get-loop-location next))
57          (else value))))))
58  (define note-demands (value)
59    (case requested-loops value
60      ((fn . args) (fn args)
61                   (record-demand fn)
62                   (map args #record-demand))
63      ((case stage value (pattern vars body) (else otherwise))
64       (stage value pattern vars body otherwise)
65       (record-demand value)
66       (record-demand body)
67       (record-demand otherwise))
68      ((lambda vars body) (vars body)
69       (record-demand body))))
70  (define record-demand (value)
71    (if (computing-loop value)
72        (let ((place (get-loop-location value))
73              (key (key value)))
74          (case requested-loops (computing-loop place)
75            ((ptw fn inputs outputs) (fn inputs outputs)
76             (if (not (member key outputs))
77                 (let ((new-outputs (cons key outputs)))
78                   (update (computing-loop place)
79                           (delay (ptw fn inputs new-outputs))))))))))
80

```

FIG. 3B

```

80 (define ptw-loop
81   (lambda (fn inputs outputs)
82     (let ((output-pairs (early-mapcar (reduction-stage computation
83                                       (lambda (key) (cons key (new-array)))
84                                       outputs))))
85       (dotimes ((i 0 99))
86         (let* ((input-scalars
87                 (early-mapcar (reduction-stage computation
88                               (lambda (pair)
89                                 (let ((key (first pair))
                                      (array (second pair)))
                                  (cons key (elt array i)
                                      inputs))
                               (output-scalars (fn input-scalars)))
90                 (early-map (reduction-stage computation
91                             (lambda (pair)
92                               (let ((key (first pair))
                                      (array (second pair)))
                                  (setf (elt array i)
                                      (find key output-scalars))))
93                             output-pairs))))))
94       (early-map (reduction-stage computation
95                   (lambda (pair)
96                     (let ((key (first pair))
97                           (array (second pair)))
98                       (setf (elt array i)
99                           (find key output-scalars))))
100                   output-pairs))))))
101 (define pointwise (fn op1 op2 => result)
102   (reduction-stage computation ;; inlineable after loop fusion
103   (find (key result) (get-loop result))))
104 (define fuse-loops
105   (lambda (loop1 loop2)
106     (if (stage-eq requested-loops loop1 loop2)
107         loop1
108         (deconstruct loop-structure loop1
109           ((ptw-loop fn1 inputss1 outputs1) (fn1 inputs1 outputs1)
110            (deconstruct loop-structure loop2
111              ((ptw-loop fn2 inputs2 outputs2) (fn2 inputs2 outputs2)
112               (let ((inputs (merge inputs1 inputs2))
113                     (outputs (append outputs1 outputs2)))
114                 (ptw-loop
115                   (preserves computation
116                     (lambda (inputs) (merge (fn1 inputs) (fn2 inputs)))
117                   inputs outputs))))))))))
118 (define find
119   (reduction-stage computation ;; inlineable after loop fusion
120   (lambda (id list)
121     (deconstruct computation list
122       (cons (cons key value) rest) (key value rest)
123       (if (stage-eq computation key id)
124           value
125           (find id rest))))))
126 (define merge
127   ... like find

```

FIG. 3C

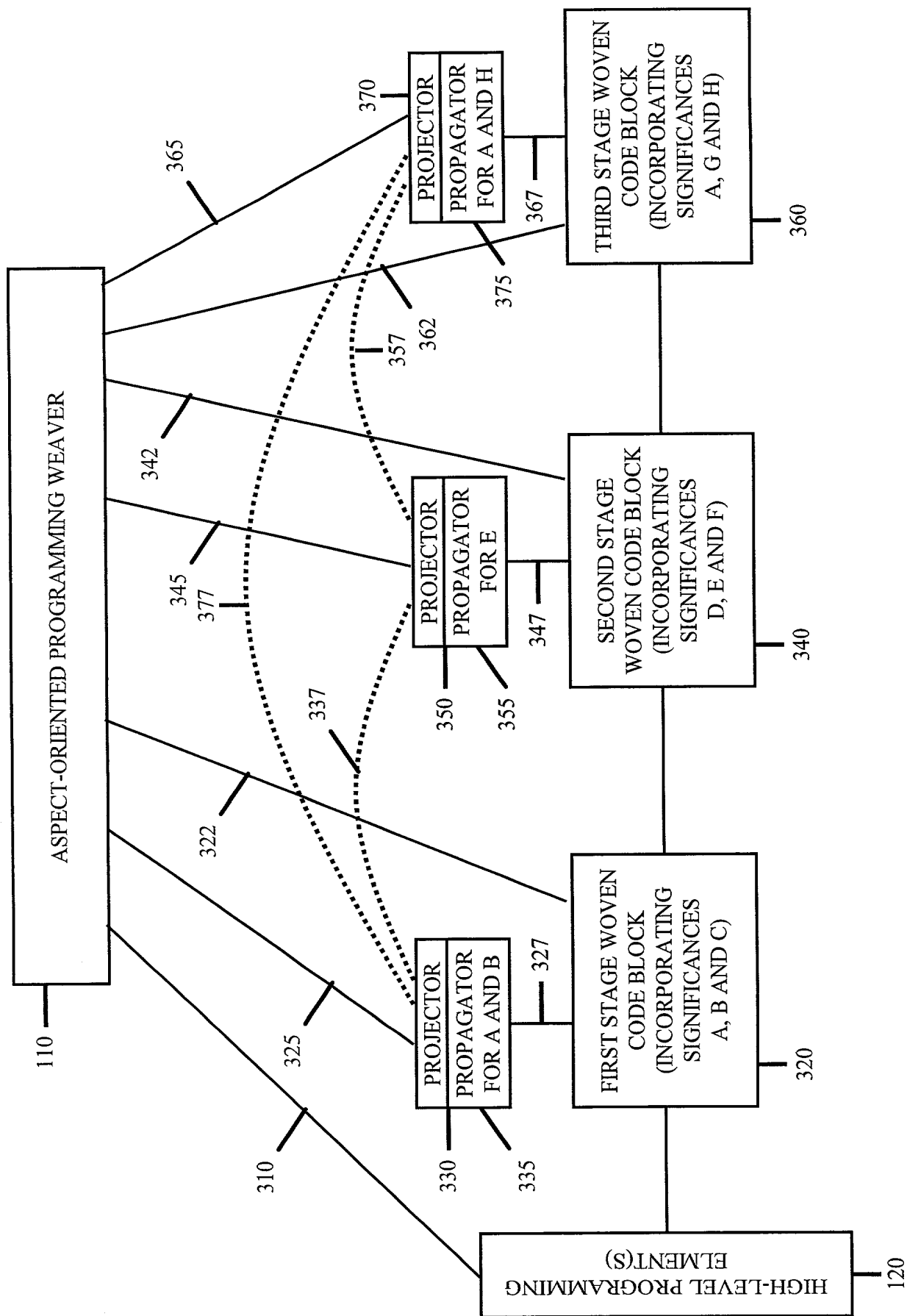


FIG. 4

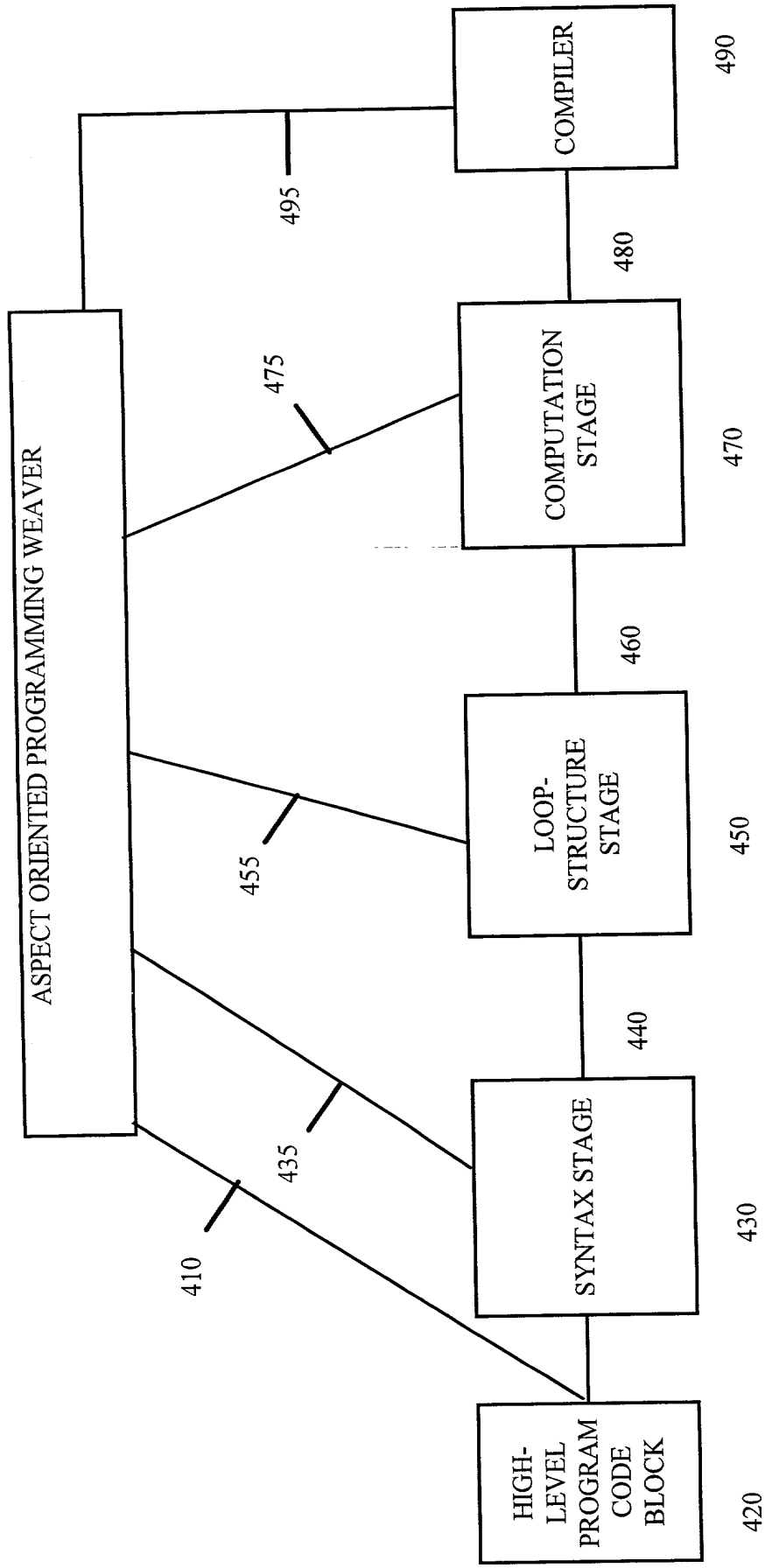


FIG. 5